

# MATH DOESN'T SUCK



## Solution Guide – Chapter 1

### Prime Numbers and Prime Factorization

#### Doing the Math from p. 8

2) 15

Well, you probably know this one from your multiplication facts, and since 3 and 5 are both prime numbers, we're done!

$$\begin{array}{c} 15 \\ \swarrow \searrow \\ (3)(5) \end{array}$$

Answer:  $15 = 3 \times 5$

3) 75

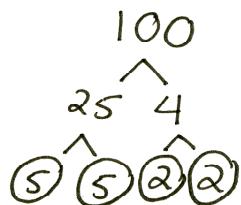
Since it ends in a 5, then you know it's divisible by 5 (see the divisibility tricks on p.9 of the book). When you divide 5 into 75, you get 15, which you know is 3 times 5. Since 3 and 5 are prime numbers, we're done!

$$\begin{array}{c} 75 \\ \swarrow \searrow \\ (5)(15) \\ \quad \swarrow \searrow \\ (3)(5) \end{array}$$

Answer:  $75 = 3 \times 5 \times 5$

4) 100

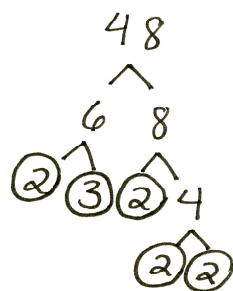
Since 100 is even, you know that 2 divides into it. But you probably also know that 25 goes into 100, 4 times. So that's a good place to start, and then it's easy to factor 25 and 4. Since 2 and 5 are both prime numbers, that's how we know we're done!



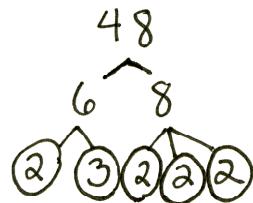
**Answer:**  $100 = 2 \times 2 \times 5 \times 5$

5) 48

You probably recognize from your multiplication facts that  $48 = 6 \times 8$ , and then it's easy to factor 6 and 8. Then we keep adding lower branches until we have only *prime* numbers left. Since 2 and 3 are both prime, that's how we know we're done. By the way, you can either factor 8 into 2 and 4, and then factor the 4 into 2's:



Or you can go ahead and factor the 8 into three 2's:



They both mean the same thing, and will give the same final answer!

**Answer:**  $48 = 2 \times 2 \times 2 \times 2 \times 3$

## Doing the Math from p. 10

2) 105

This ends in a 5, so we know that 5 is a factor. Try dividing 5 into 105, and you'll see that  $105 = 5 \times 21$ . And from our times tables, we know that  $21 = 3 \times 7$ . Done!

$$\begin{array}{c} 105 \\ \swarrow \quad \searrow \\ 5 \quad 21 \\ \quad \swarrow \quad \searrow \\ \quad 3 \quad 7 \end{array}$$

3) 540

This ends in a 0, so we know that 10 is a factor.

$$\begin{array}{c} 540 \\ \swarrow \quad \searrow \\ 10 \quad 54 \end{array}$$

Then 10 splits into its two factors, 2 and 5, and 54 as we know from our times tables, is the product of 6 and 9:

$$\begin{array}{c} 540 \\ \swarrow \quad \searrow \\ 10 \quad 54 \\ \swarrow \quad \searrow \\ 2 \quad 5 \quad 6 \quad 9 \end{array}$$

Can we keep splitting up these factors? Since 2 and 5 are prime, that tree branch is done. However, 6 is the product of 2 and 3, and 9 is the product of 3 and 3, and each of those is prime:

$$\begin{array}{c} 540 \\ \swarrow \quad \searrow \\ 10 \quad 54 \\ \swarrow \quad \searrow \\ 2 \quad 5 \quad 6 \quad 9 \\ \swarrow \quad \searrow \quad \swarrow \quad \searrow \\ 2 \quad 3 \quad 3 \quad 3 \end{array}$$

Remember, don't stop until all the numbers at the bottom of the branches are prime!  
 (note: there are often many ways to start the factoring of a number: you also could have started this one by noticing that  $5 + 4 + 0 = 9$ , which is divisible by 9, so a factor of 540 is 9, and the top two branches could have been 9 and 60, instead of 10 and 54!)

4) 1134 – Notice that  $1 + 1 + 3 + 4 = 9$ , so we know that 1134 must be divisible by 9.  
 Divide 9 into 1134 and you'll find that  $1134 = 9 \times 126$ .

$$\begin{array}{r} 1134 \\ \swarrow \quad \searrow \\ 9 \quad 126 \end{array}$$

We know that 9 “splits” into 3 and 3, but what about 126? Well, it's even, so let's divide into it by 2 and find that:  $126 = 2 \times 63$ .

$$\begin{array}{r} 1134 \\ \swarrow \quad \searrow \\ 9 \quad 126 \\ \swarrow \quad \searrow \\ 3 \quad 3 \quad 2 \quad 63 \end{array}$$

And now we know from our times tables that  $63 = 9 \times 7$ . We have to factor 9 into 3 and 3 to make sure the lowest branches are all prime, and that's it!

$$\begin{array}{r} 1134 \\ \swarrow \quad \searrow \\ 9 \quad 126 \\ \swarrow \quad \searrow \\ (3)(3) \quad 2 \quad 63 \\ \swarrow \quad \searrow \\ 7 \quad 9 \\ \swarrow \quad \searrow \\ (3)(3) \end{array}$$